# MeshStereo: A Global Stereo Model with Mesh Alignment Regularization for View Interpolation 

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#### Abstract

We present a novel global stereo model designed for view interpolation. Unlike existing stereo models which only output a disparity map, our model is able to output a $3 D$ triangular mesh, which can be directly used for view interpolation. To realize this feature, we partition the input stereo images into $2 D$ triangles with shared vertices. Lifting the $2 D$ triangulation to $3 D$ naturally generates a corresponding mesh. A technical difficulty is to properly split vertices to multiple copies when they appear at depth discontinuous boundaries. To deal with this problem, we formulate our objective as a two-layer MRF, with the upper layer modeling the splitting properties of the vertices and the lower layer optimizing a region-based stereo matching. Experiments on the Middlebury and the Herodion datasets demonstrate that our model is able to synthesize visually coherent new view angles with high PSNR, as well as outputting high quality disparity maps which rank at the first place on the new challenging high resolution Middlebury 3.0 benchmark.


## 1. Introduction

Stereo model is a key component to generate 3D proxies (either point-clouds [18] or triangular meshes [15]) for view interpolation. Mesh-based approaches are becoming more and more popular [15][16][6][20] because they are faster in rendering speed, have more compact model size and produce better visual effects compared to the point-cloud-based approaches. A typical pipeline to obtain triangular meshes consists of two steps: 1) generate disparity/depth maps by a stereo model, and 2) extract meshes from the estimated disparity maps by heuristic methods, such as triangulating

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Figure 1. A 2D triangulation and a 3D mesh of the Bowling2 test case from Middlebury 2.0 [14] generated by our approach. Blue dots in the left images denotes 2D vertices with splitting probability greater than 0.5 .
the polyline-simplified disparity regions [16].
However, due to the separation of the two steps, the obtained meshes may not be optimal for the final goal of view interpolation. The stereo matching community mainly focuses on producing disparity maps with low pixel-wise error rates $[5][9] \mid 25] \mid 23][17][12][24]$. However, pixel-wise accurate disparity maps are not necessary nor sufficient to generate high quality meshes for the task of view interpolation. Moreover, the internal structures of a mesh, e.g., alignment of adjacent triangles, which would be helpful for rendering, are not exploited.

This observation motivates us to develop an integrated approach for view interpolation, which should have two desired properties: 1) the model can naturally produce a mesh structure, such that view interpolation reduces to a simple rendering problem; 2) the model can output a corresponding disparity map with high quality to make the rendering results look as natural as possible. In this paper, we propose a stereo model that works on a 2D triangulation of an input view with these two goals in mind.

In the proposed model, an input image is first partitioned into 2D triangular regions according to edge distribution and local visual consistency, as shown in Fig. 1, with common vertices shared by adjacent triangles. To generate the
corresponding 3D triangular mesh, a key step is to properly compute the disparities of the triangle vertices. However, due to the presence of discontinuities in depth, vertices on depth boundaries should be split to different triangle planes. To model such splitting properties, we assign a latent splitting variable to each vertex. Given the split or non-split properties of the vertices, a region-based stereo approach can be adopted to optimize a piecewise planar disparity map, guided by whether adjacent triangles should be aligned or split. Once the disparity map is computed, the split or non-split properties can be accordingly updated. By iteratively running the two steps, we obtain optimized disparities of the triangle vertices. The overall energy of the proposed model can be viewed as a two-layer Markov Random Field (MRF). The upper layer focuses on the goal of better view rendering results, and the lower layer focuses on better stereo quality.

### 1.1. Contribution

The contributions of this paper are two-fold

1. We proposed a stereo model for view interpolation whose output can be easily converted to a triangular mesh in 3D. The outputted mesh is able to synthesize novel views with both visual coherency and high PSNR values.
2. In terms of stereo quality, The proposed model ranks at the first place on the new challenging high-resolution Middlebury 3.0 benchmark.

## 2. Related Work

For a comprehensive survey on two-frame stereo matching, we refer readers to the survey by Scharstein and Szeliski [14]. And for an overview of point-based view interpolation approach, we refer readers to [19]. In this section, we mainly discuss works on stereo models for imagebased rendering that make use of mesh structures.

To interpolate a new view, most of state-of-the-art view interpolation systems use multiple triangle meshes as rendering proxies [15]. A multi-pass rendering with proper blending parameters can synthesize new views in real-time [7]. Compared with the point-based rendering approaches [18], mesh-based approaches have lots of advantages, e.g., more compact model and without holes. Thus, mesh-based approaches have been a standard tool for general purpose view interpolation. Most of recent works focus on generating better meshes for existing views.

A typical pipeline to generate a triangular mesh consists of two consecutive steps: 1) run stereo matching to get a disparity map, and 2) generate a triangular mesh from the estimated map. The system presented by Zitnick et al. [26] is
one of the seminal works. In the paper, the authors first generate a pixel-wise depth map using a local segment-based stereo method, then convert it to a mesh by a vertex shader program. In [16], Sinha et al. first extract a set of robust plane candidates based on the sparse point cloud and the 3D line segments of the scene. Then a piecewise planar depth map is recovered by solving a multi-labeling MRF where each label corresponds to a candidate plane. For rendering, the 3D meshes are obtained by triangulating the polygonsimplified version of each piecewise planar region. Separation of the depth map estimation and mesh generation process is a major problem of this pipeline. The obtained triangle meshes are not optimal for rendering.

For scenes with lots of planar structures, e.g., buildings, special rendering approaches have been developed. Plane fitting is a basic idea to generate rendering proxies. Xiao and Furukawa [20] proposed a reconstruction and visualization system for large indoor scenes such as museums. Provided with the laser-scanned 3D points, the authors recover a 3D Constructive Solid Geometry (CSG) model of the scene using cuboids primitives. For rendering, the union of the CSG models is converted to a mesh model using CGAL [1], and ground-level images are texture-mapped to the 3D model for navigation. Cabral et al. [6] proposed a piecewise model for floorplan reconstruction to visualize indoor scenes. The 3D mesh is obtained by triangulating the floorplan to generate a floor mesh, which is extruded to the ceiling to generate quad facades. Rendering is done by texture mapping those triangles and quads.

Despite of the pleasant visual effects, missing of necessary details is a common problem of these plane fittingbased systems. For example, we can easily see artifacts on regions of the furniture during the navigation in the video provided by [6]. Incorporating a region-based stereo matching when generating the rendering proxies, as proposed in this paper, is a solution for the problem. Our proposed model dose not have specific assumption on scene structures, can cope with non-planar shapes, therefore can serve as a powerful plugin for [16] [6] to visualize finer structures.

To the best of our knowledge, the most related work of ours is Fickel et al. [8]. Starting from a 2D image triangulation, the method computes a fronto-parallel surface for each triangle, and then solve a linear system to adjust the disparity value on each private vertex. In mesh generation, a hand chosen threshold need to be set to classify each vertex as foreground or background. Due to the heavy frontoparallel bias, the disparity maps's quality is low. In contrast, our model produces high quality disparity maps as well as good rendering results, and does not require a hand chosen threshold in mesh generation.

Another closely related work of us is Yamaguchi et al. [23][22]. In these papers, the authors optimize a slanted plane model over SLIC segments [2], and simultaneously


Figure 2. An overview of the proposed integrated approach. 1) The input stereo pair are triangulated in image domain. 2) Piecewise planar disparity maps and the corresponding splitting probabilities of the vertices are estimated by our model. 3) The 3D meshes are lifted from the 2D triangulations according to the disparity maps and splitting properties outputted by the previous step. 4) The generated meshes are texture mapped [7], an interpolated view is synthesized by blending the projections from the two meshes to the new view angle.
reason about the states of occlusion, hinge or coplanarity over adjacent segment pairs. Although both using a slanted plane model over super-pixels, there are noticeable differences between Yamaguchi et al. and ours. 1) To exploit the latent structures of a scene, instead of modeling the relationships over segment pairs, we model the splitting probabilities over shared triangle vertices, which is a natural choice for the task of view interpolation. 2) [23] [22] performs a slanted plane smoothing on a pre-estimated disparity map, whose quality may limit the performance of the model. Our model avoids such limitation by computing matching cost based directly on photo consistency. 3) The above differences lead to completely different optimization approaches. We proposed an optimization scheme that makes use of PatchMatch [5] to achieve efficient inference in the slanted plane space.

## 3. Formulation

### 3.1. Overview

Fig. 2 illustrates the workflow of the proposed integrated approach. The basic idea is to first partition an input stereo pair to 2D triangles with shared vertices, then compute proper disparity/depth values for the vertices. With the known depth at each vertex, a 2D triangulation can be directly lifted to a 3D mesh, with shared vertices explicitly imposing the well-aligning properties on adjacent triangles. However, due to presence of depth discontinuities, vertices on depth boundaries should be split, that is, they should possess multiple depth values.

To tackle this difficulty, we model each triangle by a slanted plane, and assign a splitting probability to each vertex as a latent variable. Joint inference of the planes and the latent variables takes edge intensity, region connectivity and photo-consistency into consideration. The problem is formulated as a two layer continuous MRF with the following properties

1. Given the splitting variables, the lower layer is an MRF w.r.t. the set of plane equations, which is a regionbased stereo model imposing photo consistency and normal smoothness.
2. The upper layer is an MRF w.r.t. the set of splitting probabilities, which provides a prior on the splitting structure of the triangulation given an image.
3. The two layers are glued together by an alignment energy which encourages alignment among neighboring triangles on continuous surface, but allows splitting at depth discontinuous boundaries.

### 3.2. The Lower Layer on Stereo

Notations. We parameterize the plane equation using the normal-depth representation: each triangle $i$ is assigned a normal $\mathbf{n}_{i}=\left(n_{x, i}, n_{y, i}, 1\right)^{\top}$, and a disparity $d_{i}$ of its barycenter $\left(\bar{x}_{i}, \bar{y}_{i}\right)^{\top}$. We use $\mathbf{N}, \mathbf{D}$ to denote the set of normals and disparities collected from all triangles. Note that we fix the $n_{z}$ of a normal to 1 , since this parameterization does not harm the plane's modeling capability, and enables a closed-form update in section 4.2.1. More details can be found in supplementary materials.

Matching Cost. The overall matching cost is defined as the sum of each individual slanted plane cost

$$
\begin{align*}
E_{\text {MatchingCost }}(\mathbf{N}, \mathbf{D}) & =\sum_{i} \rho_{\text {TRIANGLE }}\left(\mathbf{n}_{i}, d_{i}\right)  \tag{1}\\
& =\sum_{i} \sum_{p \in \operatorname{Tri}_{i}} \rho\left(\left[\begin{array}{c}
p_{x} \\
p_{y}
\end{array}\right],\left[\begin{array}{c}
p_{x}-\mathcal{D}_{i}(p) \\
p_{y}
\end{array}\right]\right)
\end{align*}
$$

where $\mathcal{D}_{i}(p)=a_{i} p_{x}+b_{i} p_{y}+c_{i}$ is the disparity value at pixel $p$ induced by triangle $i$ 's plane equation. The plane coefficients $a_{i}, b_{i}, c_{i}$ are converted from their normal-depth representation by $a=-\frac{n_{x}}{n_{z}}, b=-\frac{n_{y}}{n_{z}}, c=\frac{n_{x} \bar{x}_{i}+n_{y} \bar{y}_{i}+n_{z} d_{i}}{n_{z}}$ and $\rho(p, q)$ is the pixel-wise matching cost defined by

$$
\begin{align*}
\rho(p, q)= & {\text { hamdist }\left(\operatorname{Census}_{1}(p)-\operatorname{Census}_{2}(q)\right)}+\omega \cdot \min \left(\left\|\nabla I_{1}(p)-\nabla I_{2}(q)\right\|, \tau_{\text {grad }}\right)
\end{align*}
$$

where Census ${ }_{1}(p)$ represents a $5 \times 5$ census feature around $p$ on image $I_{1}$ and hamdist $(\cdot, \cdot)$ is the hamming distance. $\nabla$. denotes the gradient operator. The values of $\tau_{\text {grad }}, \omega$ are determined by maximizing the survival rate in the leftright consistency check of the winner-takes-all results on the training images.

Normal Smoothness. We impose a smoothness constraint on the normal pairs of neighboring triangles with similar appearances

$$
\begin{equation*}
E_{\text {NormalSmooth }}(\mathbf{N})=\sum_{i, j \in \mathcal{N}} w_{i j}\left(\mathbf{n}_{i}-\mathbf{n}_{j}\right)^{\top}\left(\mathbf{n}_{i}-\mathbf{n}_{j}\right) \tag{3}
\end{equation*}
$$

where $w_{i j}=\exp \left(-\left\|\mathbf{c}_{i}-\mathbf{c}_{j}\right\|_{1} / \gamma_{1}\right)$ measures the similarity of the triangles' mean colors $\mathbf{c}_{i}, \mathbf{c}_{j}$, and $\gamma_{1}$ controls the influence of the color difference to the weight.

### 3.3. The Upper Layer on Splitting

Notations. Each shared vertex $s$ is assigned a splitting probability $\alpha_{s}$. Splitting probabilities of all 2D vertices are denoted by $\boldsymbol{\alpha}$.

Prior on the Splitting Probabilities. We model the prior by a data term and a smoothness term

$$
\begin{align*}
& E_{\text {SplitPenalty }}(\boldsymbol{\alpha})=\sum_{s} \alpha_{s} \cdot \tau_{s}  \tag{4}\\
& E_{\text {SplitSmooth }}(\boldsymbol{\alpha})=\sum_{s, t \in \mathcal{N}} w_{s t}\left(\alpha_{s}-\alpha_{t}\right)^{2} \tag{5}
\end{align*}
$$

where the penalty $\tau_{s}$ is set adaptively based on the evidence of whether $s$ is located at a strong edge. $s, t \in \mathcal{N}$ means $s$ and $t$ are neighboring vertices, and $w_{s t}$ is a weight determined by the distance of the visual complexity levels of location $s$ and $t$. The data term encourages splitting if $s$ is on a strong edge. The smoothness term imposes smoothness if $s$ and $t$ are of similar local visual complexities. Specifically

$$
\begin{align*}
\tau_{s} & =\exp \left(-\left\|\nabla I^{3}\left(x_{s}, y_{s}\right)\right\|_{1} / \gamma_{2}\right)  \tag{6}\\
w_{s t} & =\exp \left(-\left\|k\left(x_{s}, y_{s}\right)-k\left(x_{t}, y_{t}\right)\right\| / \gamma_{3}\right) \tag{7}
\end{align*}
$$

where $\left\{I^{l}, l=1,3,5,7,9\right\}$ is a sequence of progressively gaussian-blurred images using kernel size $l \times l . k(x, y)$ is largest scale that pixel $(x, y)$ 's color stay roughly constant

$$
\begin{equation*}
k(x, y)=\underset{j}{\operatorname{argmax}}\left\{\left\|I^{l}(x, y)-I(x, y)\right\|_{2}<10, \forall l \leq j\right\} \tag{8}
\end{equation*}
$$

We discuss how $\gamma_{2}, \gamma_{3}$ are set in the experiment section.

### 3.4. Gluing the Two Layers

So far the two layers have defined two global models for the two sets of variables (i.e., the plane equations and the splitting probabilities), we further combine them together through an alignment term. The new term demands a strong alignment on shared vertices located at continuous surfaces, while allows a shared vertex to posses multiple depth values if its splitting probability is high

$$
\begin{align*}
& E_{\text {Alignment }}(\mathbf{N}, \mathbf{D}, \boldsymbol{\alpha})=\sum_{s}\left(1-\alpha_{s}\right) \\
& \cdot \sum_{i, j \in G_{s}} \frac{1}{2} w_{i j} \cdot\left(\mathcal{D}_{i}\left(x_{s}, y_{s}\right)-\mathcal{D}_{j}\left(x_{s}, y_{s}\right)\right)^{2} \tag{9}
\end{align*}
$$

```
Algorithm 1 Optimize \(E_{\text {ALL }}\)
    RandomInit( \(\mathbf{N}, \mathbf{D}) ; \quad \alpha=\mathbf{1}\);
    repeat
        M-step: fix \(\boldsymbol{\alpha}\), minimize \(E_{\text {LOWER }}\) with respect to \(\mathbf{N}, \mathbf{D}\)
        by Algorithm 2 .
        E-step: fix \(\mathbf{N}, \mathbf{D}\), minimize \(E_{\text {UPPER }}\) with respect to \(\boldsymbol{\alpha}\)
        by solving (13) using Cholesky decomposition.
    until converged
```

where $G_{s}$ denotes the set of triangles sharing the vertex $s$, and recall that $\mathcal{D}_{i}\left(x_{s}, y_{s}\right)$ defined in (1) denotes disparity of $s$ evaluated by triangle $i$ 's plane equation. Therefore, at regions with continuous depth ( $\alpha_{s}$ close to zero), the alignment term will encourage triangles to have their disparities agreed on $s$. At depth discontinuous boundaries ( $\alpha_{s}$ close to 1), it allows the triangles in $G_{s}$ to stick to their own disparities with little penalty.

Note that $E_{\text {NormalSmooth }}$ and $E_{\text {Alignment }}$ together impose a complete second-order smoothness on the disparity field. That is, the energy terms do not penalize slanted disparity planes.

### 3.5. Overall Energy

Combining the two layers and the alignment energy, we obtain the overall objective function

$$
\begin{aligned}
& E_{\mathrm{ALL}}(\mathbf{N}, \mathbf{D}, \boldsymbol{\alpha})=E_{\text {MatchingCost }}+\lambda_{\mathrm{NS}} \cdot E_{\text {NormalSmooth }}(10) \\
& \quad+\lambda_{\mathrm{AL}} \cdot E_{\mathrm{Alignment}}+\lambda_{\mathrm{SP}} \cdot E_{\mathrm{SplitPenalty}}+\lambda_{\mathrm{SS}} \cdot E_{\mathrm{SplitSmooth}}
\end{aligned}
$$

where $\lambda_{\times}$are scaling factors. For the ease of presentation in the next section, we introduce the following notations

$$
\begin{gather*}
E_{\mathrm{UPPER}}=\lambda_{\mathrm{SP}} E_{\text {SplitPenalty }}+\lambda_{\mathrm{SS}} E_{\text {SplitSmooth }}+\lambda_{\mathrm{AL}} E_{\text {Alignment }}  \tag{11}\\
E_{\mathrm{LOWER}}=E_{\text {MatchingCost }}+\lambda_{\mathrm{NS}} E_{\text {NormalSmooth }}+\lambda_{\mathrm{AL}} E_{\text {Alignment }} \tag{12}
\end{gather*}
$$

## 4. Optimization

The overall energy $E_{\text {ALL }}$ in 10p poses a challenging optimization problem since the variables are all continuous and tightly coupled. We propose an EM-like approach to optimize the energy, in which the splitting probabilities $\boldsymbol{\alpha}$ are treated as latent variables, and the plane equations $\mathbf{N}, \mathbf{D}$ are treated as model parameters. Optimization proceeds by iteratively updating $\boldsymbol{\alpha}$ (E-step), which can be solved in closed-form, and $\mathbf{N}, \mathbf{D}$ (M-step), which is optimized by a region-based stereo model through quadratic relaxation. The method is summarized in Algorithm 1

### 4.1. E-Step: Optimize $E_{\text {UPPER }}$

By fixing $\mathbf{N}, \mathbf{D}$, Optimizing $E_{\text {ALL }}$ is equivalent to optimize $E_{\text {UPPER }}$, which is listed as follow with some algebraic
rearrangement

$$
\begin{equation*}
\min _{\boldsymbol{\alpha}} \sum_{s}\left(\tau_{s}-c_{\mathrm{AL}}(s)\right) \alpha_{s}+\sum_{s, t \in \mathcal{N}} w_{s t}\left(\alpha_{s}-\alpha_{t}\right)^{2}+\sum_{s} c_{\mathrm{AL}}(s) \tag{13}
\end{equation*}
$$

where $c_{\mathrm{AL}}(s)=\sum_{i, j \in G_{s}} \frac{1}{2} w_{i j} \cdot\left(\mathcal{D}_{i}\left(x_{s}, y_{s}\right)-\mathcal{D}_{j}\left(x_{s}, y_{s}\right)\right)^{2}$ is the current alignment cost at vertex $s$. And $\sum_{s} c_{\mathrm{AL}}(s)$ is now a constant independent of $\alpha$. Since (13) is quadratic in $\boldsymbol{\alpha}$, we can update $\boldsymbol{\alpha}$ in closed-form by solving the positive semi-definite linear system obtained by setting the derivatives of (13) to zeros. We solve the linear system using Cholesky decomposition.

### 4.2. M-step: Optimize $E_{\text {LOWER }}$

By fixing $\boldsymbol{\alpha}$, Optimizing $E_{\text {ALL }}$ is equivalent to optimize $E_{\text {LOWER }}$

$$
\begin{align*}
\min _{\mathbf{N}, \mathbf{D}}\{ & E_{\text {MatchingCost }}(\mathbf{N}, \mathbf{D})+\lambda_{\mathrm{NS}} E_{\text {NormalSmooth }}(\mathbf{N}, \mathbf{D}) \\
& \left.+\lambda_{\mathrm{AL}} E_{\text {Alignment }}(\mathbf{N}, \mathbf{D})\right\} \tag{14}
\end{align*}
$$

However, this subproblem is not yet directly solvable due to the non-convexity of $\rho\left(\mathbf{n}_{i}, d_{i}\right)$. Inspired by [25][21], we adopt the quadratic splitting technique to relax the energy

$$
\begin{align*}
& \min _{\mathbf{N}, \mathbf{D}, \widetilde{\mathbf{N}}, \widetilde{\mathbf{D}}} E_{\text {RELAXED }}(\mathbf{N}, \mathbf{D}, \widetilde{\mathbf{N}}, \widetilde{\mathbf{D}})  \tag{15}\\
\equiv & \min _{\mathbf{N}, \mathbf{D}, \widetilde{\mathbf{N}}, \widetilde{\mathbf{D}}}\left\{E_{\text {MatchingCost }}(\widetilde{\mathbf{N}}, \widetilde{\mathbf{D}})+\frac{\theta}{2} E_{\text {Couple }}(\mathbf{N}, \mathbf{D}, \widetilde{\mathbf{N}}, \widetilde{\mathbf{D}})\right. \\
& \left.+\lambda_{\mathrm{NS}} E_{\text {NormalSmooth }}(\mathbf{N}, \mathbf{D})+\lambda_{\mathrm{AL}} E_{\text {Alignment }}(\mathbf{N}, \mathbf{D})\right\}
\end{align*}
$$

in which

$$
\begin{equation*}
E_{\text {Couple }}(\mathbf{N}, \mathbf{D}, \tilde{\mathbf{N}}, \widetilde{\mathbf{D}})=\sum_{i}\left(\boldsymbol{\Pi}_{i}-\widetilde{\boldsymbol{\Pi}}_{i}\right)^{\top} \Sigma\left(\boldsymbol{\Pi}_{i}-\widetilde{\boldsymbol{\Pi}}_{i}\right) \tag{16}
\end{equation*}
$$

where $\boldsymbol{\Pi}_{i}=\left[\mathbf{n}_{i}^{\top}, d_{i}\right]^{\top}$, and $\Sigma=\operatorname{diag}\left(\sigma_{n}, \sigma_{n}, \sigma_{n}, \sigma_{d}\right)$ controls the coupling strength between $\boldsymbol{\Pi}_{i}$ and $\widetilde{\boldsymbol{\Pi}}_{i}$. As the $\theta$ in (15) goes to infinity, minimizing $E_{\text {RELAXED }}$ is equivalent to minimizing $E_{\text {LOWER }}$. We found that increasing $\theta$ from 0 to 100 in ten levels using the smooth step function offers good numerical stability. The values of $\sigma_{d}, \sigma_{n}$ are set to the inverse variances of the disparities and normals respectively from the training images.

### 4.2.1 Optimize $E_{\text {RELAXED }}$

We propose an algorithm similar to that in [25] to optimize the relaxed energy. The algorithm operates by alternatively updating $\widetilde{\mathbf{N}}, \widetilde{\mathbf{D}}$ and $\mathbf{N}, \mathbf{D}$, which is summarized in Algorithm 2

Update $\widetilde{\mathbf{N}}, \widetilde{\mathbf{D}}$. By fixing $\mathbf{N}, \mathbf{D}$, Problem 15 , reduces to

$$
\begin{equation*}
\min _{\widetilde{\mathbf{N}}, \widetilde{\mathbf{D}}}\left\{E_{\text {MatchingCost }}(\widetilde{\mathbf{N}}, \widetilde{\mathbf{D}})+\frac{\theta}{2} E_{\text {Couple }}(\mathbf{N}, \mathbf{D}, \widetilde{\mathbf{N}}, \widetilde{\mathbf{D}})\right\} \tag{17}
\end{equation*}
$$

```
Algorithm 2 Optimize \(E_{\text {LOWER }}\)
    set \(\theta\) to zero
    repeat
        repeat
            Minimize (17) by PatchMatch [4][5].
            Minimize \(\overline{18}\) by Cholesky decomposition.
        until converged
        Increase \(\theta\)
    until converged
```

This is a Nearest Neighbor Field (NNF) searching problem in disparity plane space, which can be efficiently optimized by PatchMatch [5][4].

Update $\mathbf{N}, \mathbf{D}$. By fixing $\widetilde{\mathbf{N}}, \widetilde{\mathbf{D}}$, problem 15 , reduces to

$$
\begin{align*}
\min _{\mathbf{N}, \mathbf{D}} & \left\{\frac{\theta}{2} E_{\text {Couple }}(\mathbf{N}, \mathbf{D}, \widetilde{\mathbf{N}}, \widetilde{\mathbf{D}})\right.  \tag{18}\\
& \left.+\lambda_{\mathrm{NS}} E_{\text {NormalSmooth }}(\mathbf{N}, \mathbf{D})+\lambda_{\mathrm{AL}} E_{\text {Alignment }}(\mathbf{N}, \mathbf{D})\right\}
\end{align*}
$$

It is easy to verify that all the three terms in (18) are quadratic in $\mathbf{N}, \mathbf{D}$ (details in supplementary materials). Therefore the update can be done in closed-form by Cholesky decomposition. Note that different from [25], we are working on triangles instead of image pixels. Therefore the update is much faster and scales to large size images.

## 5. Rendering

### 5.1. Triangulation and Mesh Generation

We propose a simple but effective method for image domain triangulation. First we partition the input image into SLIC [2] segments and perform a joint polyline simplification on each segment boundary. Second the output is obtained by delaunay triangulating each polygonized SLIC segment. We also try other triangulation approach, such as the one presented in Fickel et al. [8]. We refer interested readers to [8] for details.

Given the estimated piecewise planar disparity map and the splitting variables, a 3D mesh is lifted from the triangulation, where vertices with splitting probabilities $>0.5$ are split to multiple instances, or merged to their median value otherwise. This results in a tightly aligned mesh and there is no hand-chosen thresholds involved in contrast to Fickel et al. [8]. Fig. 3 shows example 3D meshes generated by our model.

### 5.2. View Interpolation

Given a stereo pair $I_{L}, I_{R}$ and their corresponding meshes, we now want to synthesize a new view at $\mu$ between the pair, where $0 \leq \mu \leq 1$ denotes the normalized distance from the virtual view $I_{M}$ to $I_{L}$ (with $\mu=0$ the position of $I_{L}$, and $\mu=1$ the position of $I_{R}$ ). First we


Figure 3. 2D image triangulations and 3D meshes from Middlebury 2.0 generated by our approach. Blue dots in the first row represent triangle vertices with splitting probabilities greater than 0.5. Test cases from left to right are (Babyl, Bowling2, Middl, Plastic, Rocksl) respectively. Results on Baby1,Bowling2 uses our proposed triangulation method, results on Midd1, Plastic, Rocks1 use the one in [8].


Figure 4. Sensitivity and convergence analysis. (a)-(c) show that the results are not sensitive to $\gamma_{1}, \gamma_{2}, \gamma_{3}$. (d) and (e) depict the error rate and energy against the number of iterations, with different numbers of inner loops when solving $E_{\text {LOWER }}$.
perform projective texture mapping on the proxy meshes, then the interpolated view is rendered by blending the projections of two meshes on the new angle $I_{M}$
$I_{M}(x, y)=(1-\mu) I_{L}^{\mu}(x, y) \delta_{L}(x, y)+\mu I_{R}^{\mu}(x, y) \delta_{R}(x, y)$
where $I_{L}^{\mu}$ is the projection of the mesh of $I_{L}$ at position $\mu$, and $\delta_{L}(x, y)=1$ if $I_{L}^{\mu}(x, y)$ is valid, and is 0 otherwise. $I_{L}^{\mu}$ and $\delta_{R}$ are defined analogly.

## 6. Experiments

To balance the subenergies, we employ the structured SVM [11] to the learn the weights $\lambda_{\mathrm{AL}}, \lambda_{\mathrm{DS}}, \lambda_{\mathrm{NS}}, \lambda_{\mathrm{SP}}$, $\lambda_{\text {SS }}$, where these parameters are optimized using the subgradient descent approach in [11] during training. We use five test cases Art, Motorcycle, Pipes, Shelves, Teddy from Middlebury 3.0 as training images. For the three parameters $\gamma_{1}, \gamma_{2}, \gamma_{3}$ which may need hand tuning, we found the results are not sensitive to their values. As shown in figure 4 (a)-(c), when $\gamma_{1}, \gamma_{2}, \gamma_{3}$ vary in the active range of their corresponding exponents, the average error rates vary in less than 1.0 percentage, and we set $\gamma_{1}=30, \gamma_{2}=60, \gamma_{3}=0.8$ according to the sensitivity figures. Figure4(d)-(e) provide a convergence analysis of the optimization framework, with different numbers of iterations when increasing $\theta$ in the in-
ner loop of Alg. 2. The energy decreases steadily as iteration goes by. As expected, larger number of inner iterations shows faster convergence. The most dominant drops of both the error rate and the energy happen during the first three iterations. The error rate stays relatively stable after the first three iterations while the energy continues to decrease gently. This phenomenon is expected as at later stages the error rate is not able to reveal subtle changes less than 1.0 disparity.

### 6.1. Rendering Results

Fig. 6 presents a comparisons of rendering results on the Middlebury 2.0 and the Herodion dataset $\mathbb{S}^{1}$ with ground truth intermediate views. Following Fickel et al. [8], we use VSRS3.5 [18] to generate interpolated view using disparity maps estimated by [24][12] as baselines, which are referred as VSRS-Nonlocal and VSRS-Volume. Compared to the point-based approaches (VSRS), our integrated approaches produces better visual effects, for example the surrounding of the reeindeer's neck; the text "Pattern Recognition" on the book, and the calibration pattern on the wall of the Herodion test case. Fig. 5 shows a comparisons of the stereo

[^1]|  | Aloe | Baby1 | Books | Bowling2 | Cloth3 | Lamp.2 | Laundry | Reindeer | Rocks1 | Wood2 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| VSRS-Volume | 26.13 | 27.45 | 24.20 | 26.02 | 25.75 | 28.88 | 21.67 | 25.03 | 28.46 | 29.76 |
| VSRS-Nonlocal | 25.86 | 28.39 | 25.83 | 27.47 | 25.97 | 30.99 | 24.03 | 26.03 | 29.63 | 31.47 |
| Triangle-Nonlocal | 27.01 | 31.61 | 28.35 | 30.14 | 31.39 | 31.50 | 27.04 | 27.34 | 34.35 | 31.50 |
| Fickel et al. | 27.69 | 32.15 | 28.41 | 30.10 | 31.31 | 31.76 | 27.82 | 27.70 | 34.45 | 33.28 |
| Ours | $\mathbf{2 9 . 3 4}$ | $\mathbf{3 5 . 8 4}$ | $\mathbf{3 0 . 0 7}$ | $\mathbf{3 3 . 1 6}$ | $\mathbf{3 5 . 0 5}$ | $\mathbf{3 6 . 2 8}$ | $\mathbf{2 8 . 6 6}$ | $\mathbf{3 1 . 9 7}$ | $\mathbf{3 5 . 9 5}$ | $\mathbf{3 7 . 7 2}$ |

Table 1. Comparison of PSNR values of the rendering results from sampled test cases on Middlebury 2.0.


Figure 5. Comparisons of estimated disparity maps on the Herodion datasets.
quality on the Herodion datasets. Compared to Fickel et al. [8], our approach generates cleaner disparity maps and sharper depth edges. Both [8] and ours are using the same rendering pipeline, however, our approach produces higher PSNR in all cases because of the better stereo quality.

Table 1 provides a comparisons on ten sampled test cases from Middlebury 2.0 in terms of PSNR. Our model outperforms other approaches for all test cases. Also notice in all the cases, the mesh-based approaches (including Fickel et al), produce higher PSNR than the point-based approaches, which demonstrates the advantages of using mesh structure. Moreover, with the reconstructed 3D meshes, rendering can be done much faster (0.1s) than VSRS (1s). Among the mesh-based approaches, we compare our results to Triangle-Nonlocal, which constructs the 3D meshes using the pre-estimated disparity maps from [24] by plane fitting. In all the cases, we obtain higher PSNR results, which demonstrates the advantages of the "integrated" approach compared to the "separated" one.

### 6.2. Stereo Results

We evaluated our model on the new Middlebury 3.0 [13] benchmark and currently ranks at the first place. Middlebury 3.0 is a new challenging benchmark suited with 30 high resolution test cases divided into training and test sets, including stereo pairs with different exposures, lighting conditions and slight rectification errors. Fig. 7 shows a comparison of the estimated disparity maps between SGM [10], Yamaguchi et al. [23] and our method, with corresponding error rates listed on Table 2. Our approach outperforms all the other approaches in all sampled test cases, including Yamaguchi et al. [23], which also uses a slanted plane model over super-pixel $\sqrt{2}$, Our model also produces

[^2]|  | Adiron. | Motor. | Piano | Playt. | Recyc. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Ours | $\mathbf{7 . 1}$ | $\mathbf{9 . 4}$ | $\mathbf{1 5 . 4}$ | $\mathbf{1 3 . 3}$ | $\mathbf{1 3 . 5}$ |
| Yamaguchi [23] | 8.1 | 10.6 | 19.0 | 15.3 | 13.6 |
| PatchMatch [5] | 8.1 | 11.0 | 17.4 | 16.2 | 14.3 |
| SGM [10] | 15.3 | 10.9 | 16.4 | 15.8 | 14.6 |

Table 2. Bad pixel rates of sampled test cases evaluated at 1-pixel error thresholds on Middebury 3.0.
depth discontinuities that are more respectful to the ground truth scene structure, such as the mug handle in Adirondack, and the left boundary of the dustbin in Recycle. In the experiment we use 8000 triangles, and each test case takes about 60s on CPU. The source code is available for readers to reproduce our results.

Contribution of the Latent Variables. To verify that the latent splitting variables do help improve the stereo quality, we compare our model with PatchMatch [5], which is essentially Eq. (1) in our formulation. To ensure fairness, both methods uses the same triangulation. As shown in Table 2, with the help of the splitting variables, our model improve the error rates of PatchMatch by 2.0 on average.

## 7. Conclusion

We have presented a global stereo model for view interpolation. Compared with existing stereo-based view interpolation approaches, where disparity map computation and mesh generation are separated into two steps, our approach integrates the two processes in a unified model. The proposed model is able to generate high quality disparity maps as well as synthesize new view angles with high visual coherency. Evaluations on the challenging Middlebury 3.0 benchmark demonstrated its excellent performance.


Figure 6. Comparisons of view interpolation results on Reindeer, Books, Herodion datasets. Red digits at top right corners denote PSNR values. Blue boxes in the images denotes selected failed regions (best viewed zooming in).


Figure 7. Results on the high resolution Middlebury 3.0 [13] benchmark with ground truth (Adirondack, Motorcycle, Piano, Playtable, Recycle). Test cases are of averaged size $1400 \times 1000$.

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[^1]:    ${ }^{1}$ The Herodion array generates a video stream from 22 synchronized uncompressed images operating at 30 Hz on a single PC [3], courtesy from Fickel et al. [8].

[^2]:    ${ }^{2}$ We use the publicly available code of [23] and set the preferred number of super-pixels to 8000 for fairness.

